## Interplay between Water and TiO<sub>2</sub> Anatase (101) Surface with Subsurface Oxygen Vacancy

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The interaction between water and the TiO<sub>2</sub> anatase (101) surface with a subsurface  $V_0$  is studied using first-principles calculations. Upon water adsorption, the relative stability of the subsurface and surface  $V_0$ reverses. The surface  $V_0$  becomes energetically more stable than its subsurface counterpart, which induces  $V_0$  to migrate from the subsurface to the surface with a very low energy barrier. Then the adsorbed water molecule can easily dissociate through a barrierless pathway facilitated by surface  $V_0$ . This reaction pathway has a similar energy barrier with another pathway under which water dissociates with the presence of subsurface  $V_0$  followed by  $V_0$  migration from the subsurface layer to the surface layer, indicating that subsurface  $V_0$  can facilitate water dissociation directly, or, via surface  $V_0$  indirectly. This novel interplay between the adsorbate and substrate defects may provide a new way to explain the origin of the activity of anatase (101) in photocatalysis in aqueous surroundings.

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TiO<sub>2</sub> is an inexpensive, nontoxic, metal oxide with applications in a wide range of areas, such as photocatalysis and self-cleaning materials [1,2]. The adsorption and dissociation of water on TiO<sub>2</sub> surfaces have brought a particular intensive research interest because it is the preliminary step for water-splitting [1] and water-gas shift reactions [3]. Besides TiO<sub>2</sub> rutile [4], TiO<sub>2</sub> anatase only attracted scientists' research interests in recent years due to the difficulty in obtaining a large size anatase crystal [5]. When the particle size is less than 11 nm [4], anatase is the most stable TiO<sub>2</sub> phase among brookite, anatase, and rutile-the three most common TiO<sub>2</sub> phases-and is believed to be catalytically more active than rutile [6]. The (101) surface is the predominant anatase surface due to its lower surface energy compared with other minor surfaces [e.g., the (001) or (100) surface]. Thereby, a full understanding of the interplay between the predominant (101) surface and water molecules is crucial for further study of the reactivity of anatase nanoparticles.

Water adsorption on the stoichiometric anatase (101) surface has been studied since the 1990s. Molecular adsorption has been confirmed to be energetically more favorable than dissociative adsorption by experimental and theoretical methods [5,7]. It is known that surface defects can affect a material's activity substantially by exposing low-coordinated surface atoms [8]. For example, with the combination of experimental and theoretical efforts, the abundant surface oxygen vacancies ( $V_0^{sur}$ 's) on the TiO<sub>2</sub> rutile (110) surface have been proved unambiguously to be the active sites for water dissociation [8,9]. In contrast with rutile,  $V_0$ 's on the anatase (101) surface are unstable. Because of the difficulty of forming  $V_0^{sur}$ 's, there are only

scattered experiments about O<sub>2</sub> and formic acid interacting with a defective anatase (101) surface [10-12]. While for water adsorption a recent study based on diffuse reflectance infrared Fourier transform spectroscopy (DRIFTS) suggests dissociation of water on a defective anatase (101) surface [13]. And, there is overwhelming theoretical evidence that shows water can dissociate over the  $V_0^{\text{sur's}}$  or several types of steps [14–16]. Interestingly, a recent scanning tunneling microscopy (STM) study by He et al. found  $V_0$ 's are predominant on the subsurface region of anatase (101) [17]. The following theoretical and experimental studies confirmed that subsurface oxygen vacancies  $(V_0^{sub}'s)$  are energetically more stable than  $V_{\rm O}^{\rm sur's}$ , and  $V_{\rm O}$  migration barriers from the surface layer to the subsurface layer range from 0.6 to 1.2 eV, depending on the immediate environment [18,19]. For water adsorption on the surface with  $V_0^{\text{sub}}$ , density-functional theory (DFT) calculations showed that molecular adsorption configuration remains energetically more stable than the dissociative one, with enhanced adsorption strength comparing to the stoichiometric surface, and a facile dissociation pathway with energy barrier of 0.26 eV was also identified [20], which is still waiting for experimental confirmation.

The relative stability of surface and subsurface  $V_{\rm O}$  could be reversed with the adsorption of small molecules on the surface. Setvín *et al.* first discovered an extraordinary interaction between O<sub>2</sub> and  $V_{\rm O}^{\rm sub}$  on TiO<sub>2</sub> anatase (101) with joint experimental and theoretical efforts [11]. Their results showed that the  $V_{\rm O}^{\rm sub}$  migrates to surface upon O<sub>2</sub> adsorption, and then induces O<sub>2</sub> to form a bridging (O<sub>2</sub>)<sub>O</sub> species via a low barrier of 47 meV. Considering the importance of  $(O_2)_O$  as the intermediate in the photooxidation of water [21], this interaction "could contribute to the higher photocatalytic activity of anatase relative to rutile" [21]. Besides  $O_2$ , the adsorption of perylene with a carboxylic acid anchor group could also reverse the relative stability between  $V_O^{sur}$  and  $V_O^{sub}$  to make  $V_O^{sub}$  no longer prevail [22].

In this Letter, the novel interplays between water and  $TiO_2$  anatase (101) with  $V_O^{sub}$  are proposed theoretically. The adsorption of the water molecule on the surface with  $V_0^{\text{sub}}$  decreases its relative stability compared to the surface with  $V_0^{\text{sur}}$ , which induces  $V_0^{\text{sub}}$  to bubble up to the surface to become  $V_0^{\text{sur}}$  with a low energy barrier. Then  $V_{\Omega}^{sur}$ , in turn, facilitates the dissociation of the water molecule through a barrierless pathway, forming two bridging hydroxyl groups along the  $[11\overline{1}]$  direction. To our knowledge, this novel interplay between water and substrate has not been reported previously. Meanwhile, another energetically competitive pathway of water dissociation with the presence of  $V_0^{sub}$  followed by  $V_0$  migration from the subsurface layer to the surface layer is also presented. These findings may provide an alternative explanation of the activity of the anatase (101) surface in photocatalysis in aqueous surroundings and enrich our knowledge about molecule adsorption on the metal oxide surface.

Calculations are carried out using spin-polarized DFT with the generalized gradient approximation (GGA) of Perdew-Burke-Ernzerhof (PBE) implemented in the VASP code [23–25]. Starting with a lattice parameter of a = 3.73and c = 9.37 Å [26], we obtained a = 3.78 and c =9.45 Å after full relaxation of the unit cell. A model structure with three O-Ti-O layers is used to simulate the  $TiO_2$  anatase (101) surface. The bottom layer is fixed to mimic the bulk structure. A(1 \* 4) supercell with 144 atoms exposes a surface area of  $10.18 * \times 15.13$  Å<sup>2</sup>. A vacuum layer of 20 Å is used to exclude the influence of vertical periodic images. Because of the large supercell, k-point sampling is restricted to the  $\Gamma$  point. The interaction between core and valence electrons is described by projector augmented wave method with an energy cutoff of 400 eV [27,28]. The 3s, 3p, 3d, and 4s electrons of Ti and the 2s, 2p electrons of O are considered as valence electrons explicitly. For DFT + U calculations, the on-site Coulomb repulsion parameter U for the Ti 3d orbital is set to be 3.5 eV, consistent with previous literature [10,11]. The nudged elastic band method is used for the transition state calculations [29].

Formation energy of  $V_0^{\text{sub}}/V_0^{\text{sur}}$  and water adsorption energy on stoichiometric surfaces are calculated to validate the accuracy of our results. Our calculation shows  $V_0$ formation energy in the subsurface layer is lower than that in the surface layer. The  $V_0$  formation energy is 4.18 eV for  $V_01$  (most stable surface vacancy, see Fig. 1) at the surface layer and 4.00 eV for  $V_04$  at the subsurface layer,

TABLE I. Surface and subsurface Vo formation energies.

V <sub>O</sub>	Formation energy (eV)
V <sub>0</sub> 1	4.18
V <sub>0</sub> 2	4.89
V <sub>0</sub> 3	4.54
<u>V<sub>0</sub>4</u>	4.00

quantitatively consistent with the previous calculation (4.25 and 4.03 eV, respectively) [18]. The  $V_0x$  configuration is unstable and will relax to the  $V_01$  configuration after geometry optimization. All  $V_0$  formation energies are listed in Table I. The water monomer adsorbs on the stoichiometric surface exothermally with a binding energy of -0.79 eV, consistent with the previous results of -0.73 [5] and -0.72 eV [20].

The eight surface Ti – 5*c* (five-coordinated Ti) atoms are equivalent sites for water adsorption on the stoichiometric (1 \* 4) surface supercell. But with the introduction of  $V_0^{\text{sub}}$ , five distinct adsorption sites emerge due to their relative positions to the subsurface defect (see Fig. S1 [30]).  $V_0^{\text{sub}}$ 's second nearest neighboring Ti – 5*c* (S5 in Fig. S1 [30]) is most stable for water adsorption with a binding energy of –0.84 eV. The adsorption configuration is illustrated in Fig. 2(c), denoted as  $M^{\text{sub}}$ . For adsorption energies of the rest of the adsorption sites, please refer to Table SI [30].

The water adsorption of the surface with  $V_0^{\text{sur}}$  is much stronger than that of the surface with  $V_0^{\text{sub}}$ . Ti – 4c and Ti – 5c in the vicinity of the surface defect have been thoroughly examined as possible adsorption sites. The Ti – 4c near  $V_0^{\text{sur}}$  [ $M_1^{\text{sur}}$  in Fig. 2(d)] is the most favorable adsorption site with a binding energy of –1.20 eV. Adsorption of water induces substantial structural relaxation. The oxygen atom just below  $V_0^{\text{sur}}$  moves upwards



FIG. 1 (color online). Side view of the three-layer TiO<sub>2</sub> anatase (101) surface. Five different  $V_0$  sites (numbered from  $V_01$  to  $V_04$ , and  $V_0x$ ) are also shown. Ti atoms are represented by blue (light gray) spheres; O atoms are represented by red (dark gray) spheres.



FIG. 2 (color online). Structures of the surface with  $V_0^{\text{sub}}$ ,  $V_0^{\text{sur}}$  and their relative energies are shown in (a) and (b), respectively. Structures of water adsorbed on the surface with  $V_0^{\text{sub}}$ ,  $V_0^{\text{sur}}$  and their relative energies are shown in (c) and (d), respectively. H atoms are represented by dark blue (black) spheres; Ti atoms are represented by blue (light gray) spheres; O atoms are represented by red (dark gray) spheres;  $V_0$ 's are represented by yellow (white) spheres.

substantially, breaking the Ti - O bond with the second layer Ti atom.

Dissociative adsorption configuration is more stable than molecular adsorption configuration on the surface with  $V_0^{\text{sur}}$ . The two most stable adsorption configurations,  $D_1^{\text{sur}}$ [Fig. S2(d)] and  $D_2^{\text{sur}}$  [Fig. S4(d)] [30], are identified with adsorption energy of -1.77 and -1.82 eV, respectively. The  $D_1^{\text{sur}}$  configuration is energetically more favorable than the  $M_1^{\text{sur}}$  configuration by 0.57 eV. These results are consistent with the previous results by Tilocca and Selloni [15].

For clean anatase (101),  $V_0^{\text{sub}}$  is energetically more stable than  $V_0^{sur}$  by about 0.18 eV. But the water adsorption energy of the  $M_1^{sur}$  configuration is 0.36 eV more negative than that of the  $M^{\text{sub}}$  configuration. This can be rationalized by the shorter  $O - H_W$  (hydrogen atom from water) and  $Ti - O_W$  (oxygen atom from water) bond distances of  $M_1^{\text{sur}}$  (Ti – O<sub>W</sub> : 2.14 Å; O – H<sub>W</sub> : 1.85 Å) comparing with  $M^{\text{sub}}$  (Ti – O<sub>W</sub> : 2.21 Å; O – H<sub>W</sub> : 1.99 Å). On the other hand, the stronger H<sub>2</sub>O adsorption of  $V_0^{sur}$  over  $V_0^{sub}$  could also be explained by a stronger 3d peak of Ti – 4c on surface with  $V_0^{sur}$  at the conduction band minimum compared to that of Ti - 5c on surface with  $V_{\rm O}^{\rm sub}$  (Fig. 3), and the larger downward shift of the *d*-band center of the surface with  $V_0^{sur}$  compared to that of the surface with  $V_0^{\text{sub}}$  (0.05 vs 0.04 eV). Thus, the relative stability of  $V_0^{\text{sub}}$  and  $V_0^{\text{sur}}$  is reversed after water adsorption. The surface with  $V_0^{sur}$  is 0.18 eV lower in energy than



FIG. 3 (color online). Projected density of states (DOS) of the clean surface's Ti atom where water will be adsorbed on. The DOS are aligned with their respective Fermi levels.

the surface with  $V_0^{\text{sub}}$  with water adsorption. Considering that the  $D_1^{\text{sur}}$  dissociative configuration is energetically more stable, we expect that  $V_0$  may migrate from the subsurface layer to the surface layer, and induce the adsorbed water dissociate to form two hydroxyl groups on the surface. The following transition state calculations confirmed our speculation.

The calculated V<sub>O</sub> migration pathway and atomic configurations are shown in Fig. 4. Initially, the water molecule comes close to the anatase (101) surface and adsorbs on the strongest adsorption site (S5 in Fig. S1 [30]) over  $V_0^{\text{sub}}$ with binding energy of -0.84 eV. Upon water adsorption, the relative stability of  $V_0^{\text{sub}}$  decreases and the surface reconstruction happens. By crossing a 0.09 eV energy barrier, the oxygen atom just below the surface O - 2c(two-coordinated oxygen) moves towards the subsurface defect site, breaking the Ti - O bond with the first layer Tiatom. Meanwhile, the surface Ti atom moves upward, forming a stronger bond with the water molecule. The Ti –  $O_W$  and  $O - H_W$  bond lengths reduce to 2.05 and 1.74 Å, respectively. Then the surface oxygen atom migrates to the subsurface defect site, leaving  $V_{\Omega}$  on the surface layer. The  $V_{\rm O}$  migration is followed by barrierless water dissociation with the presence  $V_0^{\text{sur}}$ , as shown in Fig. S2 [30]. It is clear  $H_W$  readily dissociates from water and migrates to its neighboring O - 2c atom. Then the OH group lies down to fill  $V_0^{\text{sur}}$ . The final state  $(D_1^{\text{sur}})$  is characterized by two bridging OH groups along the  $[11\overline{1}]$  direction.

We have also identified another energetically competitive pathway of water dissociation over  $V_0^{\text{sub}}$  (Fig. S5 [30]) followed by  $V_0^{\text{sub}}$  migration to the surface (Fig. 5). Water dissociates over  $V_0^{\text{sub}}$  after crossing a 0.12 eV energy barrier. The dissociative water induces substantial structural relaxation [Fig. 5(a)] and  $V_0$  migration to the surface layer via a barrierless pathway. Figure 5(c) shows a metastable



reaction coordinate

FIG. 4 (color online). Selected atomic configurations along the pathway for  $V_0$  migration from the subsurface to the surface with water molecularly adsorbed on the surface. H atoms are represented by dark blue (black) spheres; Ti atoms are represented by blue (light gray) spheres; O atoms are represented by red (dark gray) spheres;  $V_0$ 's are represented by yellow (white) spheres with black edges; O atoms with larger displacement are represented in dark green (black) spheres.

state structurally similar to Fig. S2(b) of [30]. The dangling OH group adsorbed on the lattice Ti atom may participate in other reactions with introduction of a reactant [13].

To verify the accuracy of the GGA results, GGA + U calculations are also performed [10,11]. The adsorption energy of the water molecule over  $V_0^{\text{sub}}$  is -0.90 eV, less stable than over  $V_0^{\text{sur}}$  by 0.07 eV. For the surface with  $V_0^{\text{sub}}$ , another energy-degenerate adsorption configuration (with one hydrogen bond between water and the surface) is identified with a binding energy of -0.93 eV (see Fig. S6 [30] for comparison with  $M^{\text{sub}}$ ), consistent with previous results [20]. Here, only  $M^{\text{sub}}$  (with two hydrogen bonds between water and the surface) is considered in the transition state calculation as a comparison with the GGA results. The migration barrier from  $V_0^{\text{sub}}$  to  $V_0^{\text{sur}}$  with molecular water adsorption is 0.15 eV. Then the adsorbed water dissociates barrierlessly, consist with GGA results. For another competitive pathway, water dissociates

pathway for  $V_0$  migration from the subsurface to the surface with water dissociatively adsorbed on the surface. H atoms are represented by dark blue (black) spheres; Ti atoms are represented by blue (light gray) spheres; O atoms are represented by red (dark gray) spheres;  $V_0$ 's are represented by yellow (white) spheres with black edges; O atoms with larger displacement are represented in dark green (black) spheres. For Fig. 5(g), the periodic image of H adsorbed on O - 2c at the left side of the image is removed for clarity.

with  $V_{\rm O}$  residing on the subsurface layer by overcoming the 0.13 eV barrier. Then the  $V_{\rm O}^{\rm sub}$  can readily migrate to the surface layer barrierlessly, similar to the result from GGA calculations. These results, together with previous calculations, show the GGA is reliable to describe the interaction between water and the reduced anatase surface [20,31].

In summary, by utilizing DFT calculation, we find a novel interplay between adsorbed water and subsurface  $V_{\rm O}$ . With H<sub>2</sub>O adsorption,  $V_{\rm O}^{\rm sur}$  becomes more stable than  $V_{\rm O}^{\rm sub}$  and can easily induce  $V_{\rm O}^{\rm sub}$  to migrate to the surface layer, which further facilitates H<sub>2</sub>O dissociation. In the meantime, another mechanism for water dissociation is also feasible. Molecular water dissociates with the presence of  $V_{\rm O}^{\rm sub}$  first, followed by  $V_{\rm O}^{\rm sub}$  migration to the surface layer. Both pathways have similar activation energy barriers, which indicate the adsorption of the water molecule on the surface with  $V_{\rm O}^{\rm sub}$  may undergo either pathways with similar possibility; in other words,  $V_{\rm O}^{\rm sub}$  can facilitate water dissociation directly or via  $V_{\rm O}^{\rm sur}$  indirectly. Considering that ample experimental evidence suggests  $V_{\rm O}^{\rm sur}$  is photocatalytically more active than  $V_{\rm O}^{\rm sub}$  [32–34],

our finding may provide an alternative way to understand the catalytic activity of anatase (101) in aqueous surroundings [35]. The catalytic activity of the anatase (101) surface not only explicitly depends on the density of  $V_0^{\text{sur}}$ , but also inexplicitly depends on the density of total  $V_0$ . As subsurface vacancies widely present on other systems (e.g., CeO<sub>2</sub>) [36], our results may also apply to these systems. Whether other molecule adsorption, for example, hydrogen or organic molecules, will introduce such  $V_0$  migration is waiting for further study.

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